

First-Principles Analysis of Cr-Doped SrTiO₃ Perovskite as Optoelectronic Materials

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Received: October 2022

Revised: March 2023

Accepted: March 2023

DOI: 10.22068/ijmse.3028

Abstract: The influence of Cr³⁺ doping on the ground state properties of SrTiO₃ perovskite was evaluated using GGA-PBE approximation. Computational modeling results inferred an agreement with the previously published literature. The modification of electronic structure and optical properties due to Cr³⁺ introducing into SrTiO₃ were investigated. Structural parameters assumed that Cr³⁺ doping alters the electronic structures of SrTiO₃ by shifting the conduction band through lower energies for the Sr and Ti sites. Besides, results showed that the band gap was reduced by approximately 50% when presenting one Cr³⁺ atom into the SrTiO₃ system and particularly positioned at Sr sites. Interestingly, substituting Ti site by Cr³⁺ led to eliminating the band gap indicated a new electrical case of transferring semiconducting material into a conducting material which intern enhance conductivity. Furthermore, it was found that Cr³⁺ doping either at Sr or Ti positions could effectively develop the SrTiO₃ dielectric constant properties. In addition, the absorption spectra was extended to cover the visible light region of the electromagnetic radiation, indicating the capability of this compound in harvesting sunlight for solar cell applications. Consequently, it can be said that Cr³⁺ is an effective dopant which opening up new prospects for various industrial and technological applications.

Keywords: Perovskite oxide-lead-free ceramics, Cr³⁺ metal doping, Band gap, Elastic constants, First-principles calculations, Optoelectronics.

1. INTRODUCTION

Strontium titanate (SrTiO₃) as lead-free ceramic is one of the perovskite oxide materials that are characterized with the stoichiometric of ABO₃ with high melting point of 2080°C. This type of materials exhibits significant characteristics [1–3]. These span a range of expedient applications for instance, in the field of microelectronics, SrTiO₃ thin films have widely been employed owing to their high dielectric constant, which promote their use as an insulating layer in integration circuits. Furthermore, due to the close lattice matches with several superconducting materials, SrTiO₃ has been considered as an epitaxial insulating layer in high T_c thin-film multilayers [4]. The wide band gap of SrTiO₃ (~3.2 eV) indicates that only a trivial part of ultra violet region (UV) can be absorbed which limits its photocatalytic performance. However, modifying the electronic structure of the host system (i.e., SrTiO₃) by doping with various metal

and non-metal elements can narrow the band gap which in turn shift the optical absorption edge from the UV to the visible light region [5]. A study has demonstrated that an enhancement in the photocatalytic property of SrTiO₃ can be attained by incorporating noble metal ions (Mn, Ru, Rh, and Ir) [6]. Heavy elements such as La and Nb have experimentally been loaded into SrTiO₃ system [7]. Results showed that altering the doping levels of La and Nb would result in reducing the thermal conductivity of 1.97 W m⁻¹ K⁻¹. It has also been reported that loading La into Ir-doped SrTiO₃ can effectively improve the photocatalytic performance under UV spectrum [8]. Mei *et al.* fabricated a novel perovskite/carbon nitride heterojunction (SrTiO₃/g-C₃N₄) to be utilized in the photocatalytic reduction of U(VI). Their findings demonstrate that perovskite-based composites can be applied in the actual environmental cleanup under visible-light to improve solar energy utilization [9]. UV-vis analysis of the

synthesized $\text{SrTi}_{1-x}\text{Cr}_x\text{O}_3$ powders revealed that the absorption spectra is extended to include UV and visible-light spectrum, while loading Chromium dopants at $x=0.00, 0.02, 0.05, 0.10$ into SrTiO_3 by replacing Ti sites [10]. Furthermore, using the polymeric precursor procedure, SrTiO_3 and Cr-doped SrTiO_3 $\text{SrTi}_{1-x}\text{Cr}_x\text{O}_3$ has been fabricated at low temperature of about 450°C . Results showed that new that when introducing Cr^{3+} into SrTiO_3 , a band gap in the visible light spectrum was generated [11]. The codoping of Cr, La with SrTiO_3 nanoparticles has been carried out by Tonda *et al.* [12]. Findings displayed that the band gap has been reduced from 3.2 eV in the UV spectrum for undoped system to 2.1 eV in the visible spectrum for Cr-codoped SrTiO_3 . However, they reported that an enhancement in the photocatalytic activity of Cr,La-codoped SrTiO_3 nanoparticles by diminishing the band gap up to 1.9 eV under sunlight radiation.

On the other hand, great deal of efforts has been dedicated on first-principles calculations represented by density functional theory (DFT) to provide an insight into the ground state properties of various metal oxides systems, involving, structural, electronic, optical, and mechanical properties [13–15]. Particularly, perovskite oxides are well investigated by DFT study that has revealed that introducing metal atoms such as, K and Na at Sr site into SrTiO_3 system would be employed as a p-type electrodes for solid-oxide fuel cell (SOFC) industry [16]. First-principles calculations have been also performed on Cr-doped SrTiO_3 to assess the consequence of Cr-doping on the band gap states and the photocatalytic activity of SrTiO_3 . Besides, to evaluate the energy required for Cr-doping, the defect formation energy is calculated. Results showed that substituting Cr for Sr site necessitates slighter formation energy than substituting Cr for Ti in the Cr-doped SrTiO_3 . Particularly, Cr-doped SrTiO_3 can absorb visible light and its photocatalytic activity improved with rising Cr^{3+} dopant contents [17]. The correlation between the oxidation state of Cr and photocatalytic performance has theoretically been investigated. The results demonstrated that the Cr^{3+} is preferably located at the Ti site which exhibits a crucial role in visible-light absorption and the improvement of photocatalytic activities of Cr-doped SrTiO_3 [18]. A DFT investigation

performed to assess the influence of Ag additive on SrTiO_3 . An improvement in the absorption spectra has been detected when introducing Ag into the SrTiO_3 system. Additionally, several results has been reported in that the energy band gap has been narrowed by 0.15 eV, the indirect band gap has been changed into direct band gap with converting the system from an n-type to a p-type semiconductor [19]. Zhou *et al.* [20] reported that adding rare earth elements (Pr, Nd, and Sm) would enhance the mechanical and dielectric properties of the strontium titanate.

To this end, the present contribution investigates the electronic and optical properties of SrTiO_3 perovskite under the framework of density functional theory calculations. Furthermore and for the first time the influence of substituting Sr and Ti atoms by chromium (Cr^{3+}) at two different dopant concentrations of (0.125 and 0.250) on the optical properties (reflectivity, absorption, dielectric function, and conductivity) of the resultant configuration was extensively studied and represents the novelty of this study. In addition, charge distribution and formation energy have also been reported. The improvement in the optical properties is ascribed to the insertion of Cr^{3+} which stimulates various optoelectronic fields.

2. EXPERIMENTAL PROCEDURES

2.1. Computational Approach

In this investigation, Cambridge Serial Total Energy Package (CASTEP) software was implemented to study the electronic, structural and optical properties of Cr-doped SrTiO_3 . A super cell of $2 \times 2 \times 2$ (40-atom/ 8-Sr, 8-Ti, and 24-O) has been constructed from the original optimized unit cell then optimization process to achieve the lowest energy configurations has been carried out. In the optimization criteria, Generalized Gradient Approximation (GGA) reported by Perdew Burke and Ernzerhof (PBE) (GGA- PBE) has been utilized for the considered arrangements [21]. The cut-off energy was fixed at 370 eV. Energy tolerance convergence was set at 5×10^{-6} eV/atom and in the Brillouin zone a k-points of $3 \times 3 \times 3$ as a Monkhorst-Pack grid was deployed [22] [23]. Ultrasoft pseudopotentials was chosen in the calculations. The valence electron configurations for Sr, Ti, Cr, and O, imply to [Kr] $5s^2$, [Ar] $3d^2 4s^2$, $3d^5 4s^1$, and $2s^2$

$2p^4$, respectively. The maximum displacement accuracy corresponds to 1×10^{-3} Å. The max stress tolerance corresponds to 0.05 GPa. To imitate the experimentally measured band gap of pure SrTiO_3 perovskite, scissor operator [24] was fixed at 1.37 eV. Finally, to evaluate the stability of the selected configurations, the defect formation energy (E_f) has been considered using the following expression;

$$E_{\text{Sr}_k\text{Ti}_l\text{Cr}_n\text{O}_m} = \frac{1}{k+l+n+m} (E_{\text{Sr}_k\text{Ti}_l\text{Cr}_n\text{O}_m} - k \times E_{\text{Sr}} - l \times E_{\text{Ti}} - n \times E_{\text{Cr}} - m \times E_{\text{O}}) \quad (1)$$

Where the constants k , l , n and m , denote the molar fractions of elements Sr, Ti, Cr, and O correspondingly. The replacement steps were fulfilled at $x = 0.125$, and 0.250 . This infers that at $x = 0.125$, only single Sr atom has been replaced by Cr^{3+} while at $x = 0.250$, two Sr atoms have been exchanged by Cr^{3+} . Following the same procedure and content, Cr atoms were positioned at Ti sites.

3. RESULTS AND DISCUSSION

3.1. Structural Relaxation and Analysis

For the conventional unit cell of SrTiO_3 , the atomic positions of Sr, Ti, and O correspond to (0,

0, 0), (0.5, 0.5, 0.5) and (0.5, 0, 0.5), respectively. Sr and Ti cations ensure considerably varied sizes where Sr exhibits higher atomic radius than Ti. The Sr and Ti cations accommodate the corner and the center of the cube, correspondingly, and the oxygen anions are positioned at the center of the cube edges.

The constructed $2 \times 2 \times 2$ configurations are shown in Figures 1-2(a-d) which is ordered according to the chromium atom's contents and positions. The crystal structure of perovskite SrTiO_3 reveals cubic unit cell with Pm3m space group [25]. The structural and electronic properties are documented in Table 1. The lattice parameters of the studied systems displayed in the table agreed with the published literature demonstrating that the considered model can reproduce the structural properties of SrTiO_3 [26–28].

3.2. Electronic Modification Analysis

Generally, the perovskite oxides exhibit significantly ionic bonding character in addition to covalent nature. The ionic radius of Sr, Ti, and Cr refer to 1.44 Å, 0.605 Å, and 0.615 Å, respectively.



Fig. 1. The crystal structure of pure and Cr-doped perovskite SrTiO_3 configurations.



Fig. 2. The crystal structure of pure and Cr-doped perovskite SrTiO_3 configurations.

Table 1. The optimized lattice parameters (\AA), band gap energy (eV), and charge distribution (e) for pure and Cr-loaded SrTiO_3 configurations.

Geometry	Loading, x	Lattice parameters (\AA)	Formation Energy (eV)	Band gap energy (eV)	Charge distribution (e)			
					Sr	Ti	Cr	O
Undoped SrTiO_3	0	Present 3.94 Exp. 3.90 [27] Cal. 3.94 [26]	–	3.20 Exp. 3.25 [28] Cal. 3.57 [26]	1.38	0.85	–	-0.74
$\text{SrTi}_{1-x}\text{Cr}_x\text{O}_3$	0.125	a=3.94	-7.96	0.00	1.39	0.825	0.53	-0.73
$\text{SrTi}_{1-x}\text{Cr}_x\text{O}_3$	0.250	a=3.93	-7.94	0.00	1.41	0.800	0.47	-0.70
$\text{Sr}_{1-x}\text{Cr}_x\text{TiO}_3$	0.125	a=3.94	-7.97	1.61	1.385	0.87	0.92	-0.735
$\text{Sr}_{1-x}\text{Cr}_x\text{TiO}_3$	0.250	a=3.93	-7.95	1.43	1.377	0.89	0.95	-0.757

Charge distribution on atoms of the molecules is an important electronic analysis as it provides information about chemical bonds between atoms in the molecule. Positive values of the cation charges in undoped and Cr^{3+} -doped SrTiO_3 demonstrate a covalent trend between them, whereas negative values of O atoms reveals an ionic tendency between these anion atoms and the cations in the studied systems. Moreover, (Sr or Ti) atoms replaced by Cr exhibit loss of their charges. However, O atoms gain more charges magnitudes as cation sites engaged by Cr^{3+} . To understand the influence of the Cr atom

incorporation at Ti and Sr sites on the electronic properties of SrTiO_3 , the total and partial density of states (DOSs) have been calculated for pure configuration as depicted in Figure 4. The plot displays that the valence band (VB) is mainly consists of the O-2p states whereas the conduction band (CB) is mostly occupied by 3d states. Figure 5 portrays the electronic DOSs for Cr-doped SrTiO_3 at Ti site. The energy band gap of the pure system which is amounted to 3.20 eV (Figure 4 and Table1) has been canceled when Cr atoms introduced and occupied Ti position in the structure as Figure 5 displayed.



Fig. 3. Charge analysis of pure and Cr-doped SrTiO_3 configurations.

As a result, this work reports that Cr-doped SrTiO_3 at Ti sites with Cr^{3+} atomic load of 0.125 and 0.250 demonstrate a conducting character.

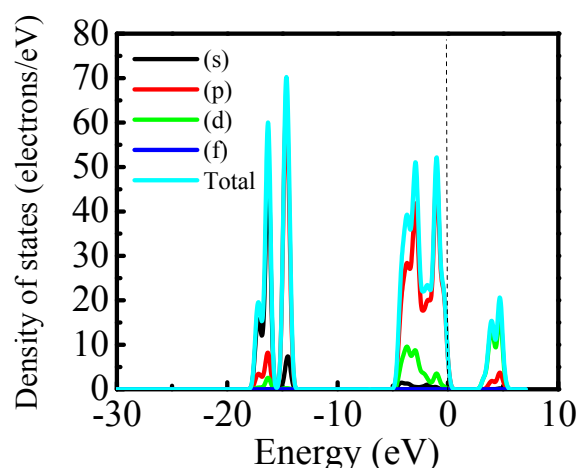


Fig. 4. The total and partial density of states for pure SrTiO_3 system. The dashed line corresponds to the Fermi level.

Suggesting that the electronic band gap has been

canceled when Cr^{3+} atoms were located at Ti bulk site shifting the material from semiconducting into conducting that exhibits metallic behavior as literature stated that Cr doping induces a transition from insulator/semiconductor to metal [29].

From other side, SrTiO_3 incorporated Cr at Sr sites remains as a semiconducting material but with less energy gap values tabulated in Table 1 and displayed in Figure 6. In addition, the calculated band gap energies correspond to 1.61 eV and 1.43 eV for the structure when Sr atomic locations being occupied by Cr^{3+} atoms at atomic ratios of 0.125 and 0.250, respectively. Those band gaps are located in the range of visible wavelength.

3.3. Optical Characteristics

It is well known that for a material to be utilized in the optoelectronic and photovoltaic fields, optical behavior is crucial to provide an insight into its response to the incident electromagnetic radiation. This performance can be elucidated by

several wavelength dependent factors, terms as, reflectivity, absorption, the real $\epsilon_1(\omega)$ and imaginary components $\epsilon_2(\omega)$, of the dielectric constants [30]. Initially, the optical properties of pure SrTiO_3 compound has been investigated then compared with the optical properties of Cr doped SrTiO_3 compound. The distortions displayed by perovskites as a result of cation replacement could be utilized to alter and modify properties of

attention including conductivity, dielectrics, etc. Variation of optical reflectivity with photon wavelength up to 800 nm is portrayed in Figure 7. Although the reflectivity spectra of pure and incorporated systems exhibit a moderate reflectivity values in ultra violet (UV) part of electromagnetic wavelength (EMW), they demonstrate small values in the visible part of EMW.

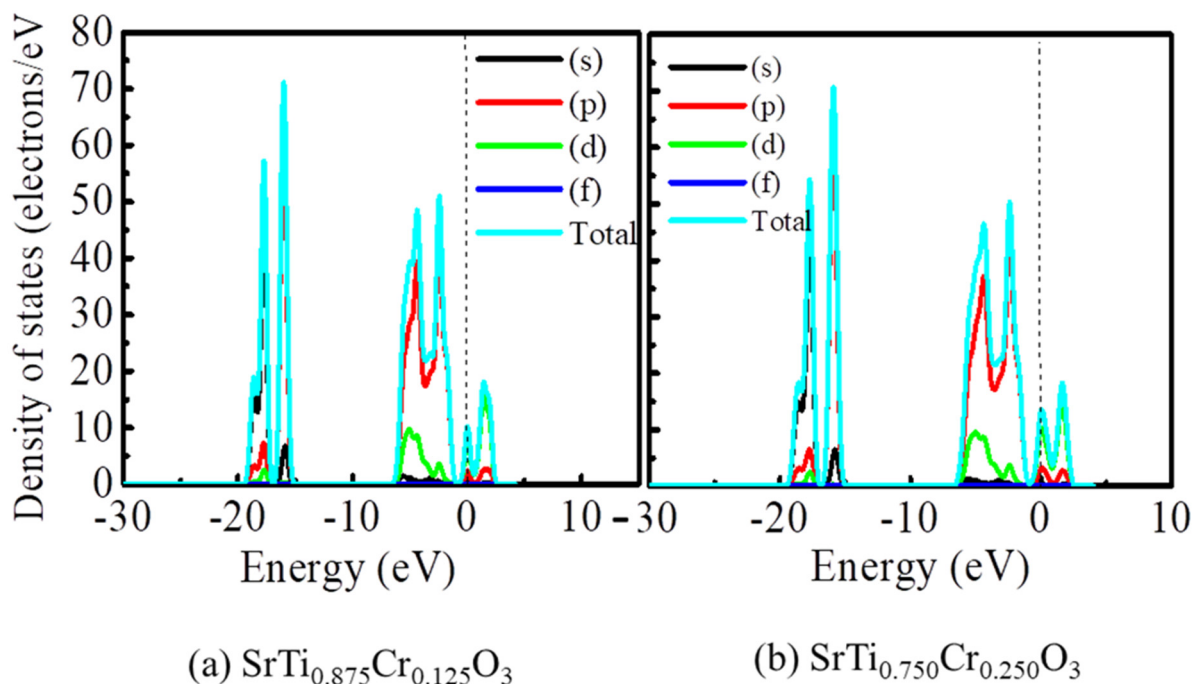


Fig. 5. The total and partial density of states Cr-doped SrTiO_3 at Ti sites. The dashed lines signify the Fermi level.

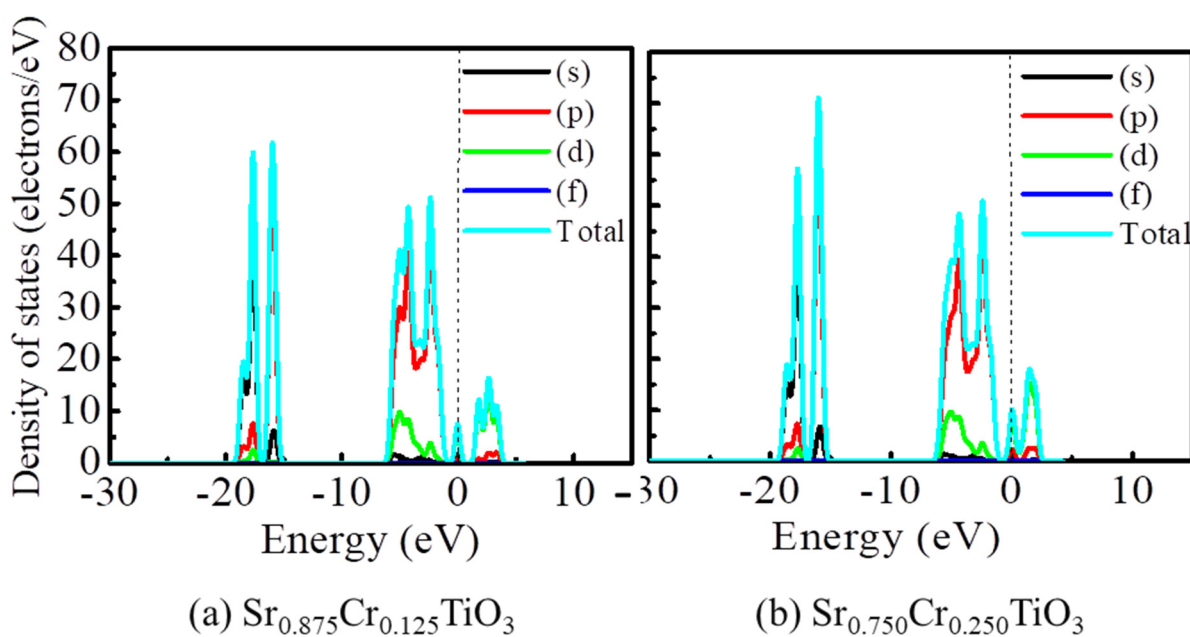


Fig. 6. The total and partial density of states Cr-doped SrTiO_3 at Sr sites. The dashed lines signify the Fermi level.

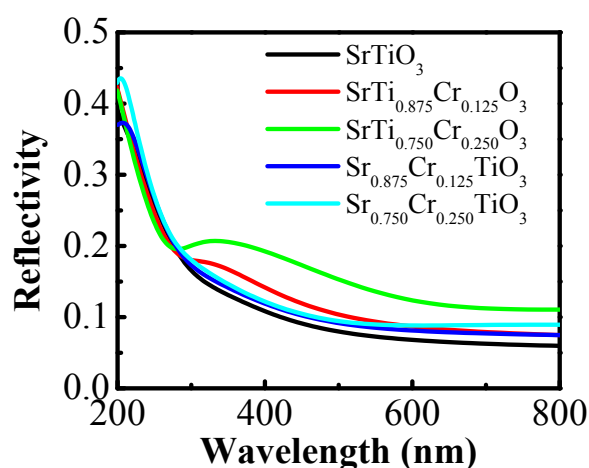


Fig. 7. The predicted reflectivity's of pure SrTiO₃ and Cr-doped SrTiO₃ structures.

Figure 8 shows the optical absorption coefficients of pure and doped SrTiO₃. Pure SrTiO₃ reveals zero absorption values in the visible range. However, an enhancement in absorption property can be evidently seen in the visible range for the Cr-introduced SrTiO₃, most notably for those configuration whose Ti sites were replaced by Cr³⁺.

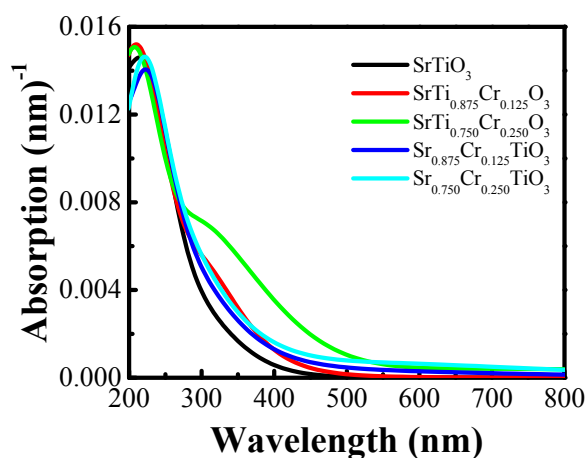


Fig. 8. The predicted absorption of pure SrTiO₃ and Cr-doped SrTiO₃ structures.

Furthermore, real part of complex dielectric constant is attained from Kramers–Kronig transformation. The real part of dielectric constant represents the polarizability of a material, whereas the imaginary part discloses the behavior of a material to be absorbing EMW incident on it and further reporting the regions of the sun rays at which the investigated material work as an absorber [31].

It can be obviously seen from Figures 9, 10 and

11 that dielectric constants, *i.e.* $\epsilon_1(\omega)$ at zero energy, of the Cr-doped configurations have higher values in reference to the pure host system value. The rise of dielectric constant is also recorded as the portion of the Cr-dopant has been risen. However, a relatively observable increase in dielectric constant noticed with the configuration that Ti atoms replaced with Cr³⁺ contents of 0.250.

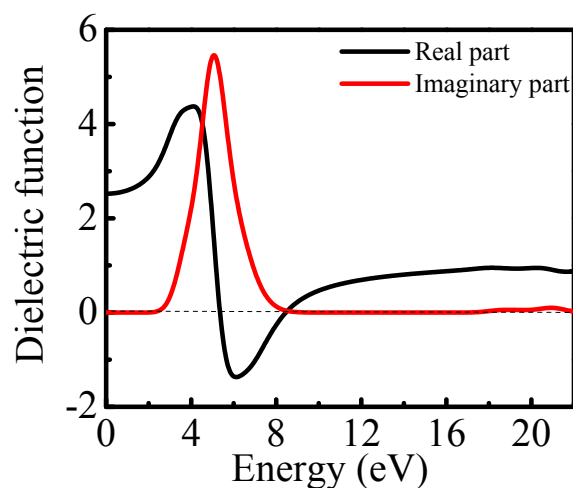


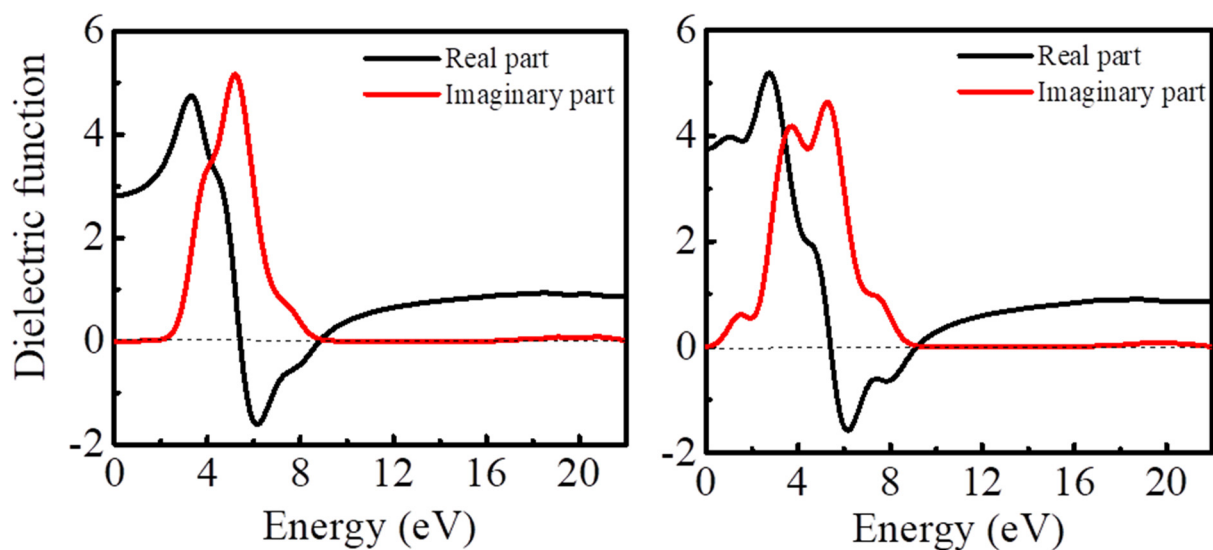
Fig. 9. The predicted dielectric function of pure SrTiO₃.

It is critical to further evaluate the optical parameters of a material in order to render a benchmarking optical performance. One such parameter can be the optical conductivity that is an indication of transferring of the electronic charges through the optical object. As depicted in Figure 12, optical conductivity of the pure SrTiO₃ incurs zero values in the visible range, emphasizing the transparency trends as absorption spectrum.

Transparency property of SrTiO₃ in visible range of EMW can be deteriorated. Swapping Ti or Sr with Cr³⁺ enhances the charge transfer occurrence of the host system in the visible region and stimulates the photovoltaic performance for the material to confidently be entering solar cell applications.

3.4. Mechanical Properties

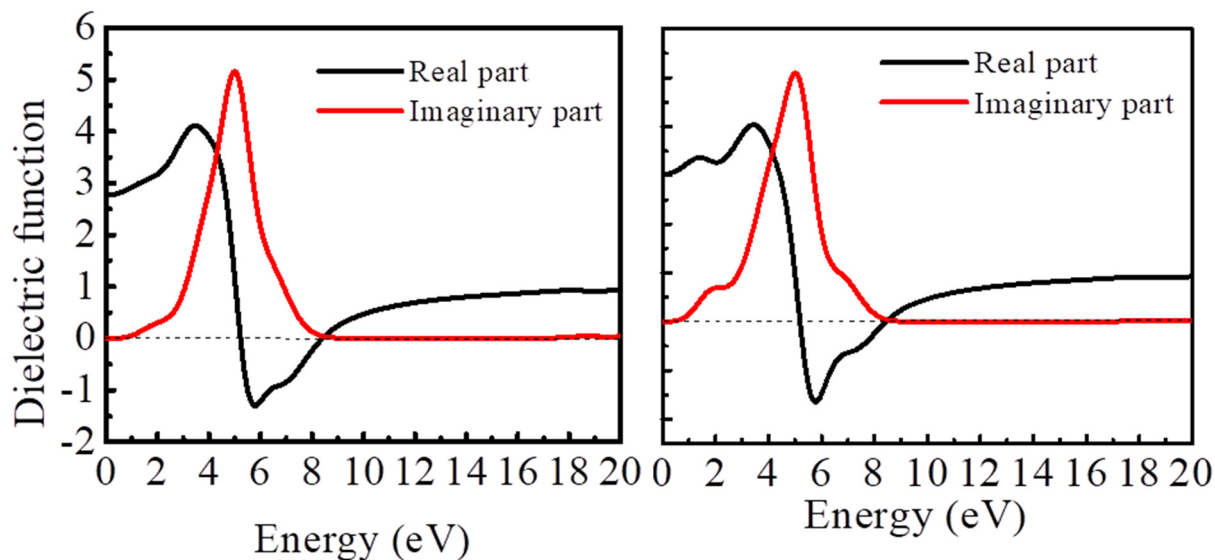
To examine the mechanical properties of bulk SrTiO₃, elastic constant (C_{ij}), bulk modulus (B), shear modulus (G), Young's modulus (E), Poisson's ratio (ν), Zener anisotropy factor (A), and B/G ratio using both GGA-PBE and LDA functionals as revealed in Table 2.



(a) $\text{SrTi}_{0.875}\text{Cr}_{0.125}\text{O}_3$

(b) $\text{SrTi}_{0.750}\text{Cr}_{0.250}\text{O}_3$

Fig. 10. The predicted dielectric function of Cr- SrTiO_3 at Ti sites.



(a) $\text{Sr}_{0.875}\text{Cr}_{0.125}\text{TiO}_3$

(b) $\text{Sr}_{0.750}\text{Cr}_{0.250}\text{TiO}_3$

Fig. 11. The predicted dielectric function of Cr- SrTiO_3 at Sr sites.

Table 2. The elastic constants C_{ij} (C_{11} , C_{12} , C_{44}), bulk modulus (B), shear modulus (G), Young's modulus (E), Poisson's ratio (ν), Zener anisotropy factor (A), and B/G ratio for the undoped SrTiO_3 configuration.

Functional	C_{11} (GPa)	C_{12} (GPa)	C_{44} (GPa)	B (GPa)	G (GPa)	E (GPa)	ν	A	B/G	
GGA-PBE	357.160	110.745	114.790	192.880	118.090	294.220	0.245	0.930	1.63 0	Present study
LDA	331.710	95.205	112.590	174.040	114.820	282.370	0.230	0.950	1.51 5	
GGA-PBEsol	350.46	101.16	111.02	184.26	116.28	288.22	0.24	0.89	1.58	Ref.[33]
Exp.				178.8						Ref.[37]



Fig. 12. The predicted conductivity of pure SrTiO₃.

The elastic constant C_{11} describes the toughness of a material versus the resulted strains, C_{12} implies the material shear stress, and C_{44} demonstrates the resistance alongside shear distortion. First-principles calculations provide a comprehensive insight into the mechanical properties of cubic perovskite oxide [32]. It is well known that bulk modulus is an indication of the resistant of the substance to compression. For the cubic system [15], bulk modulus can be evaluated from the equation below,

$$B = \frac{C_{11} + 2C_{12}}{3} \quad (2)$$

The recorded value of bulk modulus using GGA and LDA functional were in line with the available literature [33]. Another important component corresponds to shear modulus which predicts the performance and capability of a material against distortions (shape deformation) diagonally. The shear modulus (G) was assessed by employing Voigt's (G_V) and the Reuss's (G_R) approximations for the cubic system [34];

$$G_V = \frac{1}{5}(C_{11} - C_{12} + 3C_{44}) \quad (3)$$

$$G_R = \frac{5C_{44} \times (C_{11} - C_{12})}{4C_{44} + 3(C_{11} - C_{12})} \quad (4)$$

$$G = \frac{G_V + G_R}{2} \quad (5)$$

Our findings as shown in Table 2 demonstrate that SrTiO₃ highly resist shape deformation suggesting that this compound is hard. Moreover, Yong modulus refers to another significant property of a material to withstand the elongation as a reference to the original length. It has been calculated from Equation 6;

$$E = \frac{9BG}{3B + G} \quad (6)$$

The Poisson's ratio (ν) signifies the ratio of crosswise reduction tension to longitudinal

enlarging strain throughout stretching. Solid material typically exhibits Poisson's ratio ranging from 0.2-0.3. This ratio can be calculated from Equation 7.

$$\nu = \frac{3B - 2G}{6B + 2G} \quad (7)$$

The Zener anisotropy factor (A) in solid is obtained from Equation 8 [35]. A material reveals isotropic property when A equals to unity. In contrast, higher or smaller values of A indicate that the material demonstrates anisotropy character. For cubic SrTiO₃, A factor is reported to be less than 1, suggesting that SrTiO₃ is slightly anisotropy as recorded in Table 2.

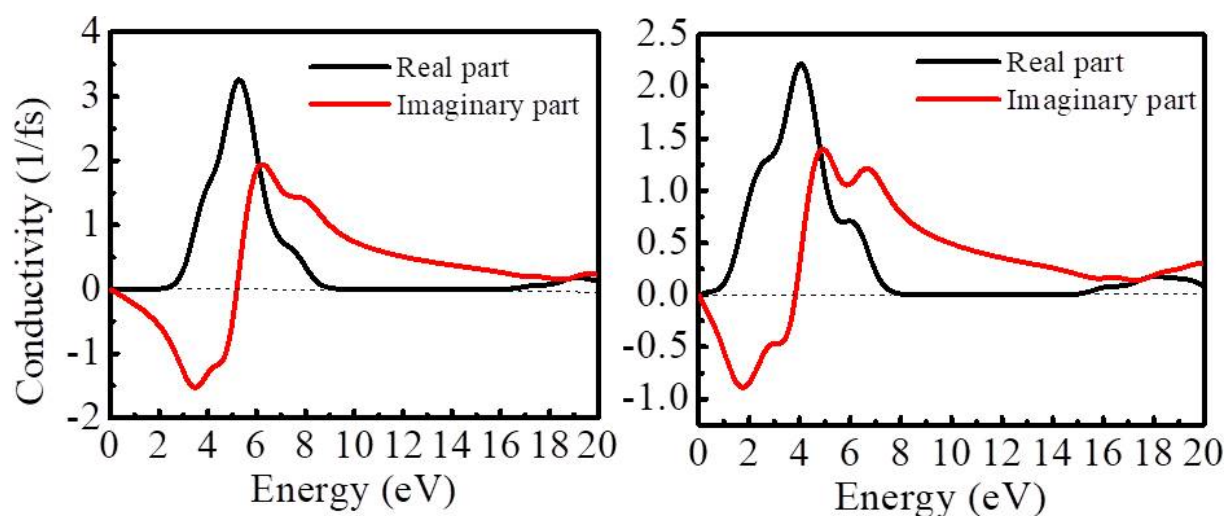
$$A = \frac{2C_{44}}{C_{11} - C_{12}} \quad (8)$$

Finally, a measurement of material's brittleness or ductility can be evaluated through B/G value [36]. A material is considered ductile at high B/G value whereas, lower values indicate that the material is brittle. Moreover, the slandered value to distinguish between ductility and brittleness correspond to 1.75. Based on this explanation, SrTiO₃ is predicted to be brittle.

4. CONCLUSIONS

Strontium titanate (SrTiO₃) is one of the perovskite materials having broad application in fields of optoelectronic industries.

This contribution provides an insight into ground state properties of pure SrTiO₃ including electronic, structure, optical, and mechanical characteristics via the state of art of first-principles calculations. Accordingly, the impact of Cr³⁺ cation doping levels at the Sr and Ti sites of SrTiO₃ on the electronic structures and optical properties was investigated. Our simulated results revealed an agreement with available experiment and predicted findings. Moreover, an adjustments on the electronic and optical properties was recorded after inserting Cr³⁺. Electronic band gap disappeared when Cr³⁺ atoms were located at Ti bulk site, transferring the material from semiconductor into conductive material, and metallic behavior. This behavior is confirmed by the literature that stated Cr³⁺ doping induces a transition from insulator/semiconductor to metal. In case of Cr³⁺ inserted into and occupied Sr positions, the host system retained its semi-conducting character, but with a gap energy on the visible region.



(a) $\text{SrTi}_{0.875}\text{Cr}_{0.125}\text{O}_3$

(b) $\text{SrTi}_{0.750}\text{Cr}_{0.250}\text{O}_3$

Fig. 13. The predicted conductivity of doped Cr-SrTiO₃ at Ti sites.



(a) $\text{Sr}_{0.875}\text{Cr}_{0.125}\text{TiO}_3$

(b) $\text{Sr}_{0.750}\text{Cr}_{0.250}\text{TiO}_3$

Fig. 14. The predicted conductivity of doped Cr-SrTiO₃ at Sr sites.

A comprehensive investigation of optical characteristics such as reflectivity, absorption, dielectric function and conductivity of the pure and Cr inserted SrTiO₃ enable us to reach a conclusion that the visible light absorption is improved by Cr³⁺ doping content. Such an outcome would support developing and designing new optoelectronics.

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